Calculato	or Model:		
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MID – YEAR EXAMINATI SECONDARY 1	ON 2017		
Mathematics		3 May 2017	
Additional Materials: Writing paper		2 hours	S
READ THESE INSTRUCTIONS FIRST			
Do not open this booklet until you are told to do so.			
Write your name, class and index number on all the work you han Write in dark blue or black pen on both sides of the paper. You may use a pencil for any diagrams, graphs or rough working. Do not use highlighters or correction fluid.			
Answer all questions in Sections A and B.			
If working is needed for any question it must be shown with the ar Omission of essential working will result in loss of marks. The use of an approved scientific calculator is expected, where ap If the degree of accuracy is not specified in the question, and if the three significant figures. Give answers in degrees to one decimal For π , use either your calculator value or 3.142, unless the quest	opropriate. he answer is r place.	-	
At the end of the examination, fasten all your work securely togeth The number of marks is given in brackets [] at the end of each of The total number of marks for this paper is 80.		art question.	
Section A : Answer the questions in the space provided.			
Section B : Answer the questions on the writing paper provided.			
	For E	Examiner's Use	
	Sectio	on A / 40	
	Sectio	on B / 40	
	Tota	al / 80	
This document consists of <u>11</u> printed page	es and <u>1</u> bla	ank page.	

Section A: Answer all the questions.

1 Round 0.999 to 2 significant figures.

Answer:[1]

- 2 (a) Calculate $\frac{0.4215^3}{\sqrt[3]{645}-3.5}$. Truncate your answer to 6 decimal places.
 - (b) Write your answer to part (a), correct to 3 significant figures.

3 Find $\sqrt[3]{1728}$ by using prime factorisation.

Answer:[3]

- 4 (a) Express 90 as a product of its prime factors, giving your answer in index notation.
 - (b) Find the smallest possible value of n such that 90n is a perfect cube.

Answer: $90 = \dots [1]$ $n = \dots [1]$

5 Consider the following numbers :

$$0, \sqrt{4}, \sqrt[3]{-27}, \frac{5}{\sqrt{3}}, 5, \frac{\pi}{4}.$$

- (a) Write down the
 - (i) irrational numbers,
 - (ii) positive integers,
 - (iii) prime numbers.
- (b) Represent all the numbers on the number line below.



- 6 (a) Express 125 g as a percentage of 5 kg.
 - (b) Find the value of 4.5% of \$8.

Answer: (a) % [2]

(b) \$[2]

7 Evaluate, without the use of a calculator, $\left[8 + (-4)^3\right] - \left[-2(12+3) \div 3\right]$, showing all your working clearly.

- 8 Simplify the following
 - (a) x(2x+3)-7(3x-1),
 - **(b)** $5a \times (-2b) \times \sqrt[3]{-125a^3}$.

- 9 Factorise the following expressions
 - (a) $15a^2b + 6ac$,
 - **(b)** (2v-w)(p+1)+2w(p+1).

Answer:	(a)	1	I

10 Given that a = 3, b = -2 and $c = \frac{1}{2}$, evaluate

(a) 2a-3c,

(b)
$$\frac{ab^2 - 3a}{c}$$
.

- A train 320 m long passes through a tunnel 5.2 km long.The average speed of the train is 28 km/h.
 - (a) Convert 28 km/h into m/s.
 - (b) Calculate the time taken for the train to pass completely through the tunnel. Give your answer in minutes.

Answer: (a) m/s [1]

(b) min [3]

- 12 A factory produces a type of baking powder made with baking soda, cream of tartar and cornstarch. The amount of baking soda, cream of tartar and cornstarch are in the ratio of 7:3:4 respectively.
 - (a) In a small bag of baking powder, there are 60g of cornstarch.What is the weight of the baking powder in the small bag?
 - (b) Bags of baking powder are filled at a rate of 180g per second.How many bags of baking powder weighing 1.5 kg each can be filled in 3.5 hours?

Answer: (a) g [2]

(b) bags [3]

End of Section A

8

Section B: Answer all the questions.

- 13 (a) Write down an algebraic expression for each of the following statements.
 - (i) Subtract 5x + 3 from $3x^2 + 5$. [2]
 - (b) Simplify the following.

(i)
$$2y - 3[x + 4(x - y)],$$
 [2]

(ii)
$$\frac{3n-m}{4} + \frac{2n-m}{5}$$
. [3]

- (c) If a: b = 5: 4 and b: c = 4.2: 0.65, find a: c. [2]
- 14 Joey paid \$28.80 for a pair of shoes after a discount of 25% from a departmental store. What is the original price of the shoes? [2]
- 15 Marcus wants to change 600 Singapore Dollars (S\$) to Thai Baht (THB). The exchange rate is S\$1 = 24.72 THB.
 - (a) Find the amount of Thai Baht (THB) Marcus will receive if he changes 600
 Singapore Dollars (S\$). [1]
 - (b) The money changer is only able to change amounts in multiples of 1000 THB. The money changer decides to round up the amount in (a) to the nearest 1000 THB.
 Find the amount in S\$ that Marcus needs to top up for the extra amount, giving [3] your answer to the nearest cent.

- 16 One pen costs *x* cents. An eraser costs 30 cents less than a pen and a ruler costs two-third of a pen.Find a simplified expression for
 - (i) the cost of an eraser in cent, [1]
 - (ii) the total cost of an examination goodie pack consisting of 3 pens, 1 eraser and2 rulers in cent. [2]
- 17 Solve the equations:

(a)
$$1 + \frac{1}{2}x = \frac{1}{5}x$$
, [2]

(b)
$$2(5y+3) = 2y+14$$
. [2]

18 Susan cycles from home to a coffeeshop to purchase dinner before continuing the journey to her grandmother's place.

Susan cycled at a speed of 4 m/s to the coffeeshop for 3 minutes, took another 10 minutes to buy dinner and continued the rest of the journey to her grandmother's house at a speed of 6 m/s. Given that the total distance travelled is 4500 m,

- (a) find the distance between Susan's house and the coffeeshop. [1]
- (b) Find the average speed for the whole journey in m/s. [3]

- 19 (a) Mr Lee was paid a monthly basic salary of \$3 850 since January 2015. At the end of 2015, he was given a bonus of 13.5% of the value of sales that he has made during the year. If the total value of his sales in 2015 was \$300 000, calculate Mr Lee's total income in 2015. [2]
 - (b) Mr Lee has to pay income tax in January 2016 for the annual income earned in 2015. The relief amount that will not be subjected to income tax is shown in the table below.

Type of relief	Amount
Personal relief	\$1000
Child relief	\$5000 each child
CPF	\$17 340
Voluntary donation	Three times the amount donated

Mr Lee has only one child and he has been making voluntary donation of \$50 every month to an approved organization. The gross tax payable for the first \$40 000 is \$550 and the tax rate for the rest is 7%. Calculate his income tax payable for 2015 using the information given above. [3]

- (c) In January 2016, Mr Lee's basic monthly basic salary was cut by \$200.
 - (i) Calculate the percentage decrease in the basic monthly salary from 2015
 to 2016, giving your answer to three significant figures. [2]
 - (ii) In 2016, he was paid a bonus of 15.5% of the value of his sales that he has made during the year. Given that his bonus in 2016 is \$33 790, calculate the total value of his sales in 2016.

20 Kale ordered one set meal at \$55.60 and an ice cream for \$12.90 at a restaurant.Below shows Kale's bill before payment.

1 set meal	\$55.60
Ice cream	\$12.90
SUBTOTAL	\$68.50
10% Service Charge	\$6.85
7% Goods and Services	\$5.27
Tax (GST)	

Currently, the restaurant is offering two discount packages that Kale can choose from.

Discount Package I:

Enjoys 10% off the subtotal of the bill, which is thereafter subjected to 10% Service Charge first and then 7% GST.

Discount Package II:

There is no service charge and the subtotal is subjected to 7% GST.

Explain, showing all necessary working, which discount package is a better option for Kale.

[5]

~ End of Paper ~

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12

	Calculator Model:		
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MID – YEAR EX SECOI	AMINATION 20	17	
Mathematics		Wednesday, 3	May 2017
			2 hours
Additional Materials: Writing paper			
READ THESE INSTRUCTIONS FIRST			
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Write your name, class and index number on all the Write in dark blue or black pen on both sides of the You may use a pencil for any diagrams, graphs or r Do not use highlighters or correction fluid.	oaper.		
Answer all questions in Sections A and B.			
If working is needed for any question it must be sho Omission of essential working will result in loss of m The use of an approved scientific calculator is expec If the degree of accuracy is not specified in the que three significant figures. Give answers in degrees to For π , use either your calculator value or 3.142, un	arks. eted, where appropriate stion, and if the answe one decimal place.	er is not exact, give	
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Section A : Answer the questions in the space provi	ded.		
<u>Section B</u> : Answer the questions on the writing pap	er provided.		
		For Examiner's L	Jse
	S	ection A	/ 40
	S	ection B	/ 40

This document consists of $\underline{9}$ printed pages and $\underline{1}$ blank page.

2

Section A: Answer all the questions.

1 Round 0.999 to 2 significant figures.

Answer: 1.0 [1]

2 (a) Calculate $\frac{0.4215^3}{\sqrt[3]{645}-3.5}$. Truncate your answer to 6 decimal places.

(b) Write your answer to part (a), correct to 3 significant figures.

(a)
$$\frac{0.4215^3}{\sqrt[3]{645} - 3.5} = 0.014568$$
 (truncated to 6 d.p.)

(b)
$$\frac{0.4215^3}{\sqrt[3]{645} - 3.5} = 0.014568$$

= 0.0146 (to 3 s.f.)

Answer : (a) 0.014568 [1]

(b) 0.0146 [1]

3 Find $\sqrt[3]{1728}$ by using prime factorisation.

2	1728	$1728 = 2^6 \ll 3^3$
2	864	
2	432	$\sqrt[3]{1728} \models \sqrt[3]{2^6} \times 3^3$
2	216	$=2^{2}\times3$
2	108	
2	54	=12
3	27	
3	9	
В	3	
	1	

Answer: 12 [3]

4 (a) Express 90 as a product of its prime factors, giving your answer index notation.(b) Find the smallest possible value of n such that 90n is a perfect cube.

$$\begin{array}{c|cccc}
2 & 90 \\
\hline
3 & 45 \\
\hline
3 & 15 \\
\hline
5 & 5 \\
\hline
& 1
\end{array}$$
90 = 2×3²×5

90n =
$$2^3 \times 3^3 \times 5^3$$

n = $2^2 \times 3 \times 5^2$
n = 300
n = 300 [1]

5 Consider the following numbers :

$$0, \sqrt{4}, \sqrt[3]{-27}, \frac{5}{\sqrt{3}}, 5, \frac{\pi}{4}$$

- (a) Write down the
 - (i) irrational numbers,
 - (ii) positive integers,
 - (iii) prime numbers.
- (b) Represent all the numbers on the number line below.



²⁰¹⁷ Mid-Year Examination/S1/Mathematics

7 Evaluate, without the use of a calculator, $\left[8 + (-4)^3\right] - \left[-2(12+3) \div 3\right]$, showing all your workings clearly.

$$\begin{bmatrix} 8 + (-4)^3 \end{bmatrix} - \begin{bmatrix} -2(12+3) \div 3 \end{bmatrix} = \begin{bmatrix} 8 + (-64) \end{bmatrix} - \begin{bmatrix} -2(15) \div 3 \end{bmatrix}$$
$$= \begin{bmatrix} 8 - 64 \end{bmatrix} - \begin{bmatrix} -30 \div 3 \end{bmatrix}$$
$$= -56 - (-10)$$
$$= -56 + 10$$
$$= -46$$

Answer : -46 [3]

8 Simplify

(a)
$$x(2x+3)-7(3x-1)$$
,
(b) $5a \times (-2b) \times \sqrt[3]{-125a^3}$.

(a)
$$x(2x+3)-7(3x-1) = 2x^2 + 3x - 21x + 7$$

= $2x^2 - 18x + 7$

(b)
$$5a \times (-2b) \times \sqrt[3]{-125a^3} = 5a \times (-2b) \times (-5a)$$

= $59a^2b$

- Answer: (a) $2x^2 18x + 7$ [2]
 - (b) 50a²b [2]

- 9 Factorise the following expressions (a) $15a^2b+6ac$,
 - **(b)** (2v-w)(p+1)+2w(p+1).
 - (a) $15a^2b + 6ac = Ba(5ab + 2c)$

(b)
$$(2v - w)(p + 1) + 2w(p + 1) = (p + 1)(2v - w + 2w)$$

= $(p + 1)(2v + w)$

Answer: (a) 3a(5ab+2c) [1]

(b) (p+1)(2v+w) [2]

²⁰¹⁷ Mid-Year Examination/S1/Mathematics

10 Given that a=3, b=-2 and $c=\frac{1}{2}$, evaluate

(a)
$$2a-3c$$
,
(b) $\frac{ab^2-3a}{c}$.
(a) $2a-3c = 2(3)-3(\frac{1}{2})$
 $= 6-\frac{3}{2}$
 $= 4\frac{1}{2} \text{ or } 4.5$

(b)
$$\frac{ab^2 - 3a}{c} = \frac{3(-2)^2 - 3(3)}{\frac{1}{2}}$$
$$= \frac{12 - 9}{\frac{1}{2}}$$
$$= 3 \times 2$$
$$= 6$$



- 11 A train 320 m long passes through a tunnel 5.2 km long. The average speed of the train is 28 km/h.
 - (a) Convert 28 km/h into m/s.
 - (b) Calculate the time taken for the train to pass completely through the tunnel. Give your answer in minutes.

$$a)\frac{28km}{1h} = \frac{28 \times 1000m}{1 \times 3600s}$$
$$= \frac{28000m}{3600s}$$
$$= 7\frac{7}{9}m/s$$

b) Total length of the tunnel and train = 5.2km + 0.32 km = 5.52 km

Time taken =
$$\frac{5.52}{28}$$

= $\frac{69}{350}h$
Time taken in minutes = 11.8 min (3 s.f) or $11\frac{29}{35}$ min

- Answer: (a) $7\frac{7}{9}$ m/s [1] (b)11.8 or $11\frac{29}{35}$ min [3]
- 12 A factory produces a type of baking powder made with with baking soda, cream of tartar and cornstarch. The amount of baking soda, cream of tartar and cornstarch are in the ratio of 7 : 3 : 4 respectively.
 - (a) In a small bag of baking powder, there are 60g of cornstarch. What is the weight of the baking powder in the small bag?
 - (b) Bags of baking powder are filled at a rate of 180g per second. How many bags of baking powder weighing 1.5 kg each can be filled in 3.5 hours?
 - (a) Weight of baking powder in the small bag $= \frac{60}{4} \times 14$ = 210g
 - (b) 3.5 hours = 12600 sec

Number of bags of V.5 kg each that can be filled in 3.5 hours = $\frac{0.18 \times 12600}{1.5}$ = 1512

> *Answer: (a)* 210 g [2] (b) 1512 bags [3]

End of Section A

7

Section B: Answer all the questions.

13 (a) Write down an algebraic expression for each of the following statements.

(i) Subtract
$$5x + 3$$
 from $3x^2 + 5$. [2]
 $3x^2 + 5 - (5x + 3) = 3x^2 + 5 - 5x - 3$
 $= 3x^2 - 5x + 2$

(b) Simplify the following:

(i) Simplify
$$2y - 3[x + 4(x - y)]$$
. [2]
 $2y - 3[x + 4(x - y)] = 2y - 3[x + 4x - 4y]$
 $= 2y - 3[5x - 4y]$
 $= 2y - 15x + 12y$
 $= -15x + 14y$

(ii)
$$\frac{3n-m}{4} + \frac{2n-m}{5}$$
. [3]
 $\frac{3n-m}{4} + \frac{2n-m}{5} = \frac{5(3n-m)}{\sqrt{20}} + \frac{4(2n-m)}{\sqrt{20}} = \frac{15n-5m+8n-4m}{20} = \frac{15n-5m+8n-4m}{20} = \frac{23n-9m}{20}$

[2]

(c) If a : b = 5 : 4 and b : c = 4.2 : 0.65, find a : c. b : c = 4.2 : 0.65= 420 : 65

$$a: b = 5: 4 \quad b: c = 420: 65$$

$$a: b = 525: 420 \quad b: c = 420: 65$$

$$a: c = 525: 65$$

$$= 105: 13$$

14 Joey paid \$28.80 for a pair of shoes from a departmental store. If the store made a [2] loss of 25%, what is the original price of the shoes?

Original price of shoes
$$=$$
 $\frac{100}{75} \times \$28.80$
 $=$ $\$38.40$

- 15 Marcus wants to change 600 Singapore Dollars (S\$) to Thai Baht (THB). The exchange rate is S¹ = 24.72 THB.
 - Find the amount of Thai Baht Marcus will receive if he uses \$\$600. **(a)** [1] S\$600 = 600 × 24.72 = 14832 THB
 - (b) The money changer is only able to change amounts in multiples of 1000 THB. [3] The money changer decides to round up the amount in (a) to the nearest 1000 THB.

Find the amount in S\$ that Marcus needs to top up for the extra amount, giving your answer to the nearest cent.

Amount that Marcus needs to top up in Thai Baht = 15000 - 14832

= 168 THB

[1]

168 THB = 8\$ 6.7971 Amount of S\$ that Marcus needs to top up = S\$6.80 (rounded to nearest cents)

One pen costs *x* cents. An eraser costs 30 cents less than a pen and a ruler costs 16 two-third of a pen.

Find a simplified expression for

(a) the cost of an eraser in cents, Cost of an eraser = (x-30) cents

2017 Mid-Year Examination/S1/Mathematics

8

(b) the total cost of an examination goodie pack consisting of 3 pens, 1 eraser and [2]2 rulers in cents.

9

Total cost of examination goodie pack =
$$3x + (x - 30) + 2(\frac{2}{3}x)$$

= $3x + x - 30 + \frac{4}{3}x$
= $(\frac{16}{3}x - 30)$ cents

17 Solve the equations:

(a)
$$1 + \frac{1}{2}x = \frac{1}{5}x$$
 [2]
 $1 + \frac{1}{2}x = \frac{1}{5}x$
 $\frac{1}{2}x - \frac{1}{5}x = -1$
 $\frac{5}{10}x - \frac{2}{10}x = -1$
 $\frac{3}{10}x = -1$
 $3x = -10$
 $x = -3\frac{1}{3}$

(b) 2(5y+3) = 2y+14. 2(5y+3) = 2y+14 $10y+6 \Rightarrow 2y+14$ 8y = 8y = 1

[2]

18 Susan cycles from home to a coffeeshop to purchase dinner before continuing the journey to her grandmother's place.

Susan cycled at a speed of 4 m/s to the coffeeshop for 3 minutes, took another 10 minutes to buy dinner and continued the rest of the journey to her grandmother's house at a speed of 6 m/s. Given that the total distance travelled is 4500 m,

(a) find the distance between Susan's house and the coffeeshop.

[1]

Distance between coffeeshop and Susan house = 4×180 = 720 m

(b) Find the average speed for the whole journey in m/s. [3] Time taken to travel from Susan to Grandma's house = $\frac{4500-720}{6}$ = 630 s 4500

Average speed for the whole journey = $\frac{4500}{180 + 630 + 600}$

$$= 3.19 (3 \text{ s.f}) \text{ or } 3\frac{9}{47} \text{ m/s}$$

[2]

19 (a) Mr Lee was paid a monthly basic salary of \$3 850 since January 2015.
 At the end of 2015, he was given a bonus of 13.5% of the value of sales that he has made during the year. If the total value of his sales in 2015 was \$300 000, calculate Mr Lee's total income in 2015.

Mr Lee's total income in
$$2015 = (3850 \times 12) + (\frac{13.5}{100} \times 300000)$$

= \$86700

(b) Mr Lee/has to pay indome tax in Vanuary 2016 for the annual income earned in [3] 2015/. The relief amount that will not be subjected to income tax is shown in the table below:

Type of relief	Amount
Personal relief	\$1000
Child relief	\$5000 each child
CPF	\$17 340
Voluntary donation	Three times the amount donated

Mr Lee has only one child he has been making voluntary donation of \$50 every month to an approved organization. The gross tax payable for the first

\$40 000 is \$550 and the tax rate for the rest is 7%. Calculate his income tax payable for 2015 using the information given above.

Amount of relief =
$$$1000 + $5000 + $17340 + 3(50 \times 12)$$

= $$25140$
Amount taxable = $$86700 - 25140
= $$61560$
Amount of tax payable = $550 + \frac{7}{100}(61560 - 40000)$
= $550 + 1509.20$
= $$2059.20$

- (c) In January 2016, Mr Lee's basic monthly basic salary was cut by \$200.
 - (i) Calculate the percentage decrease in the basic monthly salary from 2015 [2] to 2016, giving your answer to three significant figures.

Percentage decrease
$$\models \frac{200}{3850} \times 100\%$$

= 5.1948%
= 5.19% (3s.f.)

In 2016, he was paid a bonus of 15.5% of the value of his sales that he [2]

(ii) has made during the year. Given that his bonus in 2016 is \$33 790,
 calculate the total value of his sales in 2016.

Total value of sales =
$$\frac{\$33790}{15.5} \times 100$$
$$= \$218000$$

20 Kale ordered one set meals at \$55.60 and an ice cream for \$12.90 at a restaurant. [5] Below shows Kale's bill before payment.

1 set meal	\$55.60
Ice cream	\$12.90
SUBTOTAL	\$68.50
10% Service Charge	\$6.85
7% Goods and Services	\$5.27
Tax (GST)	<i>***</i> - <i>i</i>

Currently, the restaurant is offering two discount packages that Kale can choose from.

Discount Package I:

Enjoys 10% off the subtotal of the bill, which is thereafter subjected to 10% Service Charge first and then 7% GST.

Discount Package II:

10% Service Charge is waived, which is thereafter subjected to 7% GST.

Explain, showing all necessary working, which discount package is a better option for Kale.

Discount Package I:

Bill subjected to Service Charge and $GST = 90\% \times 68.50

= \$61.65.

Total amount paid in Discount Package I = $(110\% \times \$61.65) \times 1.07$

Discount Package II:

Bill subjected to GST = \$68.50

Total amount paid in Discount Package II = 68.50×1.07

= \$73.30

Since amount paid in Package II is more than amount paid in Package I, therefore Package I is a better option for Kale.

~ End of Paper ~

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